# Super Matrix Solver-P-ICCG: 

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URL: http://www.vinas.com
$>\underline{I C C G}$ is an iterative solution method for linear equations based on CG (Conjugate Gradient) method. In ICCG, the calculation speed of CG method is enhanced with pre-processing technology (Incomplete Cholesky Factorization). Compared with CG method that has no pre-processing, ICCG method is faster and more stable method.
$\Rightarrow \underline{I C C G}$ is an iterative method with many actual performance results in diverse analyses fields such as structural, electromagnetic and computational fluid dynamic analyses.
>Co-developed with Kyoto University (Academic Center for Computing and Media Studies)
$>3$ types of parallel algorithm:

- Block-ICCG
$\bullet$ Part-ICCG
- AMC-ICCG (Algebraic Multi-Color Ordering Method)
$>$ Commercialized Block-ICCG with great parallelization effect
>SMP Parallel
Easily parallelized in Windows, UNIX and Linux environment
$\star$ Makes the solver a black box on module basis for ease of use


## Performance Comparison of P-ICCG vs. SMS-AMG

P-ICCG
$\square$
Good
Good
Good
Fair-Good
Fair

SMS-AMG Good
-
-
Excellent Good

NOTE: " = " indicates items that are not accommodated.


User demands:



Greatly speed up specific calculation

## P-ICCG Summary Specifications (1)

$>$ Parallel method: accommodates shared memory type (SMP)
$>$ Object coefficient matrices: sparse matrices that are generated from discretizastion methods such as finite element, finite volume, and differential methods.
>Maximum number of CPU's: unlimited; however, 1 to 8 CPU's are recommended.
$>$ Types of unknowns:real and complex numbers
$>$ Symmetry of problems :limited to symmetric problems only (cannot calculate asymmetric problems)
$>$ Zero-diagonal problems: able to calculate ${ }^{1}$

1. cannot solve all of the problems with zero elements in diagonal

## P-ICCG Summary Specifications (2)

$>$ Environment: Windows, Unix and Linux (refer to the next page for details)
$>$ Able to be installed into programs written in computer languages such as C and Fortran ${ }^{2}$
2. Installation into programs written in other languages has not yet been confirmed.
$>$ Parameters that can be specified: convergence criteria, number of iteration, initialization condition, and so forth ${ }^{3}$
3. refer to the next page for summary of arguments; refer to the product manual for detailed information.
$>$ Program format: provided in executable module format such as DLL ${ }^{4}$
4. source code will not be disclosed
$\Rightarrow$ Accessories:manual, sample installation data, etc.

|  | OS | Recommended <br> Environment | Recommended Compiler | Environment for <br> which operation is <br> noted | Compilers for <br> which operation <br> is noted | Remarks |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- |

Example: C language

## int PICCGD( <br> double *X, double *Abrs, int *Nstp, double *AD, double *AU, double *B, int *LNT, int *LND, int ND, int NS, int Mstp, double EPS, int Lop1, int Lu0sw, double GAMMA, int COLOR );

Partial list of arguments (an excerpt from the product manual)

| Arguments | Definition (C) | $\begin{aligned} & \text { Definition } \\ & \text { (FORTRAN) } \end{aligned}$ | Dimension | Attribute | Meaning of variable <br> (at the time of input) | Meaning of variable <br> (at the time of output) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| X | double* | Real*8 | Array | I/O | Initial value of unknown $\boldsymbol{x}$ (vector) (when the value of Lu 0 sw is 4 ) | Solution of unknown $\boldsymbol{x}$ (vector) (the latest value, if not converged.) |
| Abrs | double* | Real*8 | Array | O | Set the storage area for output. <br> (For C language, pass pointers of variables.) | Achieved accuracy (in relative residual) |
| Nstp | int* | Integer*4 | Array | O |  | Actual number of iteration. |
| AD | double* | Real*8 | Array | I | Values of diagonal elements of matrix $A$ | Values after computation are not guaranteed. |
| AU | double* | Real*8 | Array | I | Values of non-diagonal, non-zero elements in upper half of matrix $\boldsymbol{A}$. |  |
| B | double* | Real*8 | Array | I | Values of right-hand side constant vector $\boldsymbol{b}$ |  |
| LNT | int* | Integer*4 | Array | I | Column indices ( j ) of non-diagonal, non-zero elements in upper half of matrix $A(i, j)$. |  |
| LND | int* | Integer*4 | Array | I | Numbers of non-diagonal, non-zero elements in each row of upper half of matrix $\boldsymbol{A}$. |  |
| ND | int | Integer*4 | Value | I | Dimension of matrix $\boldsymbol{A}$. <br> (= number of unknowns in the simultaneous equations $=$ length of array $\mathrm{X}, \mathrm{B}, \mathrm{AD}$, or LND) |  |
| NS | int | Integer*4 | Value | I | Number of non-diagonal, non-zero elements in upper half of matrix A. (= length of array AU or array LNT) |  |

## P-ICCG's Parallel Calculation Performance (1)

## >Actual Calculation Time

| Types of Problems Analyzed | Approximate |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |
| unknowns |  | Convergence Time (sec.); target convergence: norm<1.0e-10

Comparison of Calculation Performance
(1 CPU calculation speed as 1 )

| Types of Problems Analyzee | Approximate | Convergence Time (sec.) target convergence: norm<1.0e-10) |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | number of |  |  |  |  |
|  | unknowns | 1-CPU | 2-CPU | 4-CPU | 8 -CPU |
| Magnetic field analysis | 220 K | 1.0 | 2.0 | 3.3 | 6.5 |
| Fluid analysis | 500 K | 1.0 | 1.4 | 2.4 | 4.1 |
| Structural analysis | 250 K | 1.0 | 1.6 | 3.1 | 5.5 |
| Fluid analysis | 1000 K | 1.0 | 1.3 | 2.2 | 3.7 |



## P-ICCG's Parallel Calculation Performance (2)



## Data for Confirmation of P-ICCG's Performance

Calculation Time for P-ICCG Process: Electromagnetic Analysis with JMAG of Japan Research Institute

| Data No. | Data Name | Model Dimension | Real/ <br> Complex Number | Dimension | ICCG Calculation Time in hours (Ratio to 1cpu Calculation Time) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | 1cpu | 2cpu | 4cpu | 8 cpu |
| 1 | Magnetic Head | 3D | Real | 647,701 | 0.70 | $\begin{gathered} 0.37 \\ (1.89) \end{gathered}$ | $\begin{gathered} 0.24 \\ (2.92) \end{gathered}$ | $\begin{gathered} 0.19 \\ (3.68) \end{gathered}$ |
| 2 | Outer Rotor | 2D | Real | 148,959 | 7.42 | $\begin{gathered} 5.74 \\ (1.29) \end{gathered}$ | $\begin{gathered} 3.17 \\ (2.34) \end{gathered}$ | $\begin{gathered} 2.54 \\ (2.92) \end{gathered}$ |
| 3 | IPM Motor | 2D | Real | 10,899 | 0.51 | $\begin{gathered} 0.42 \\ (1.21) \end{gathered}$ | $\begin{gathered} 0.52 \\ (0.98) \end{gathered}$ | $\begin{gathered} 0.26 \\ (1.96) \end{gathered}$ |
| 4 | Conductor Cable | 2D | Real | 67,075 | 0.46 | $\begin{gathered} 0.28 \\ (1.64) \end{gathered}$ | $\begin{gathered} 0.17 \\ (2.71) \end{gathered}$ | $\begin{gathered} 0.13 \\ (3.54) \end{gathered}$ |
| 5 | Inducing Machine | 3D | Complex | 385,610 | 2.01 | $\begin{gathered} 2.33 \\ (0.86) \end{gathered}$ | $\begin{gathered} 1.55 \\ (1.30) \end{gathered}$ | $\begin{gathered} 1.09 \\ (1.84) \end{gathered}$ |
| 6 | Craw Pole Alternator | 3D | Real | 769,635 | 6.59 | $\begin{gathered} 3.28 \\ (2.01) \end{gathered}$ | $\begin{gathered} 1.70 \\ (3.88) \end{gathered}$ | $\begin{gathered} 1.42 \\ (4.64) \end{gathered}$ |
| 7 | Large Craw Pole Alternator | 3D | Real | 2,464,702 | 6.64 | $\begin{gathered} 3.03 \\ (2.19) \end{gathered}$ | $\begin{gathered} 1.79 \\ (3.71) \end{gathered}$ | $\begin{gathered} 1.83 \\ (3.63) \end{gathered}$ |
| 8 | Transformer | 3D | Real | 680,448 | 3.69 | $\begin{gathered} 2.21 \\ (1.67) \end{gathered}$ | $\begin{gathered} 1.19 \\ (3.10) \end{gathered}$ | $\begin{gathered} 0.84 \\ (4.39) \end{gathered}$ |
| 9 | Rotating Conductor | 3D | Real | 769,496 | 9.79 | $\begin{gathered} 7.52 \\ (1.30) \end{gathered}$ | $\begin{gathered} 4.35 \\ (2.25) \end{gathered}$ | $\begin{gathered} 3.30 \\ (2.97) \end{gathered}$ |

## Results of Confirmation of P-ICCG's Performance

Calculation Time for P-ICCG Process: an example of electromagnetic analysis by JMAG of Japan Research Institute


Number of CPU's

Courtesy: Japan Research Institute

## Application Example of P－ICCG（ $\mu$－tec Co．，Ltd．）

## Verified improvement by applying P－ICCG in calculation speed of $\mu$－MF1



Analysis model／

Analysis result


【Details of Analysis】
Non－linear static magnetic field analysis of
8 －pole 6－slot brushless DC motors
Number of nodes： 194724
Number of elements： 203840
Number of unknowns： 189315
【System environment】
CPU：Xeon 2．4GHz，2GB－Memory
OS：Windows XP
$\mu$－tec Co．，Ltd web site：http：／／www．mutec．org／


For further information on SMS-P-ICCG such as
-Benchmark Testing (BMT)
-Evaluation module
-Other inquiries

## Please contact:

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